

# Package ‘xegaGeGene’

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**Title** Grammatical Evolution

**Version** 1.0.0.0

**Description** Grammatical evolution (see O'Neil, M. and Ryan, C. (2003,ISBN:1-4020-7444-1)) uses decoders to convert linear (binary or integer genes) into programs. In addition, automatic determination of codon precision with a limited rule choice bias is provided. For a recent survey of grammatical evolution, see Ryan, C., O'Neill, M., and Collins, J. J. (2018) <[doi:10.1007/978-3-319-78717-6](https://doi.org/10.1007/978-3-319-78717-6)>.

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**URL** <<https://github.com/ageyerschulz/xegaGeGene>>

**Encoding** UTF-8

**RoxygenNote** 7.2.3

**Suggests** testthat (>= 3.0.0)

**Imports** numbers, xegaSelectGene, xegaBNF, xegaDerivationTrees

**NeedsCompilation** no

**Author** Andreas Geyer-Schulz [aut, cre]  
(<<https://orcid.org/0009-0000-5237-3579>>)

**Maintainer** Andreas Geyer-Schulz <[Andreas.Geyer-Schulz@kit.edu](mailto:Andreas.Geyer-Schulz@kit.edu)>

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## R topics documented:

ChoiceVector . . . . .	2
CodonChoiceBiases . . . . .	3
CodonChoiceBiasesDeprecated . . . . .	4
CodonPrecision . . . . .	5
CodonPrecisionWithThreshold . . . . .	5
IFxegaGeGene . . . . .	6

MinCodonPrecision . . . . .	7
mLCMG . . . . .	7
mLCMGCodonPrecision . . . . .	8
tLCM . . . . .	9
xegaGeDecodeGene . . . . .	10
xegaGeGene . . . . .	11
xegaGeGeneMapFactory . . . . .	13
xegaGeGeneMapmLCM . . . . .	14
xegaGeGeneMapMod . . . . .	15
xegaGeInitGene . . . . .	16
xegaGePrecisionFactory . . . . .	17
<b>Index</b>	<b>18</b>

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ChoiceVector	<i>Choice vector of a grammar.</i>
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### Description

Choice vector of a grammar.

### Usage

ChoiceVector(LHS)

### Arguments

LHS            Vector of Integers. The left-hand side G\$LHS of a grammar object G.

### Value

Vector of the number of choices for non-terminal symbols.

### See Also

Other Utility: [mLCMG\(\)](#)

### Examples

```
NT<-sample(5, 50, replace=TRUE)
ChoiceVector(NT)
```

---

CodonChoiceBiases      *Biases in Rule Choice.*

---

### Description

Measures the biases in rule choice for each non-terminal. Statistics computed:

- dP: Difference in probability between random choice with equal probability and modulo rule with a codon precision.
- dH: Difference in entropy between random choice with equal probability and modulo rule with a codon precision.

### Usage

```
CodonChoiceBiases(cv, precision)
```

### Arguments

cv	Choice vector of grammar.
precision	Number of bits of codon.

### Value

Data frame with the following columns

- \$precision: Number of bits.
- \$cv: i-th element of choice vector.
- \$dp: Deviation from choice with equal probability for \$precision.
- \$dH: Entropy difference between choice with equal probability and biased choice for \$precision.

### See Also

Other Diagnostics: [CodonChoiceBiasesDeprecated\(\)](#), [CodonPrecision\(\)](#), [tLCM\(\)](#)

### Examples

```
CodonChoiceBiases(c(1, 2, 3, 5), 3)  
CodonChoiceBiases(c(1, 2, 3, 5), 5)
```

---

CodonChoiceBiasesDeprecated

*Biases in Rule Choice (Deprecated)*

---

## Description

See CodonChoiceBiases. The use of the outer product leads to memory problems for precision>31 and becomes slow for precision>24.

## Usage

```
CodonChoiceBiasesDeprecated(cv, precision)
```

## Arguments

cv	Choice vector of grammar.
precision	Number of bits of codon.

## Value

Data frame with the following columns

- \$precision: Number of bits.
- \$cv: i-th element of choice vector.
- \$dp: Deviation from choice with equal probability for \$precision.
- \$dH: Entropy difference between choice with equal probability and biased choice for \$precision.

## See Also

Other Diagnostics: [CodonChoiceBiases\(\)](#), [CodonPrecision\(\)](#), [tLCM\(\)](#)

## Examples

```
CodonChoiceBiasesDeprecated(c(1, 2, 3, 5), 3)  
CodonChoiceBiasesDeprecated(c(1, 2, 3, 5), 5)
```

---

CodonPrecision	<i>Compute codon precision with the choice bias of rules below a threshold.</i>
----------------	---

---

**Description**

For automatic determination of the least codon precision for grammar evolution with an upper threshold on the choice bias of for the substitution of all non-terminal symbols.

**Usage**

```
CodonPrecision(cv, pCrit)
```

**Arguments**

cv	Choice vector of a context-free grammar.
pCrit	Threshold for choice bias.

**Value**

Precision of codon.

**See Also**

Other Diagnostics: [CodonChoiceBiasesDeprecated\(\)](#), [CodonChoiceBiases\(\)](#), [tLCM\(\)](#)

**Examples**

```
CodonPrecision(c(1, 2, 3, 5), 0.1)
CodonPrecision(c(1, 2, 3, 5), 0.01)
```

---

CodonPrecisionWithThreshold	<i>Precision of a codon which has a choice bias below a probability threshold.</i>
-----------------------------	--

---

**Description**

The choice bias is the sum of the absolute values of the difference between a k equally probable choices and the probability distribution of the modulo choice rule.

**Usage**

```
CodonPrecisionWithThreshold(LHS, pCrit)
```

**Arguments**

LHS	The left-hand side of a grammar object G.
pCrit	Threshold for the choice bias for single non-terminal.

**Value**

The precision of a codon which guarantees that the choice bias for all nonterminals is below a probability threshold of PCrit.

**See Also**

Other Precision: [MinCodonPrecision\(\)](#), [mLCMGCodonPrecision\(\)](#)

**Examples**

```
NT<-sample(5, 50, replace=TRUE)
CodonPrecisionWithThreshold(NT, 0.1)
CodonPrecisionWithThreshold(NT, 0.01)
```

---

IFxegaGeGene

*The local function list IFxegaGeGene.*

---

**Description**

The local function list IFxegaGeGene.

**Usage**

```
IFxegaGeGene
```

**Format**

An object of class list of length 23.

---

MinCodonPrecision	<i>Minimal precision of codon.</i>
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---

**Description**

The minimal precision of the codon needed for generating a working decoder for a context-free grammar G. However, the decoder has some choice bias which reduces the efficiency of grammar evolution.

**Usage**

```
MinCodonPrecision(LHS, ...)
```

**Arguments**

LHS	Vector of Integers. The left-hand side of a grammar object G.
...	Unused. Needed for common abstract interface of precision functions.

**Value**

Integer. The Precision of a codon whose upper bound is the least power of 2 above the maximum number of rules for a non-terminal of a grammar.

**See Also**

Other Precision: [CodonPrecisionWithThreshold\(\)](#), [mLCMGCodonPrecision\(\)](#)

**Examples**

```
NT<-sample(5, 50, replace=TRUE)
MinCodonPrecision(NT)
```

---

mLCMG	<i>Compute the mLCM of the vector of the number of production rules in a production table.</i>
-------	--

---

**Description**

Compute the least common multiple of the prime factors of the vector of the number of rules applicable for each non-terminal symbol.

**Usage**

```
mLCMG(LHS)
```

**Arguments**

LHS                    Vector of integers. The left-hand side of a grammar object G.

**Details**

For removing the bias of the modulo rule in grammatical evolution, see Keijzer, M., O'Neill, M., Ryan, C. and Cattolico, M. (2002). This version works for integer genes coded in the domain  $1:mLCM$  without bias in choosing a rule. See Keijzer et al. (2002). However, if the mLCM and  $2^k$  are relative prime, it is impossible to find an unbiased binary coding. The choice bias is considerable lower than for `MinCodonPrecision()`.

**Value**

Integer. The least common multiple of the vector of the available rules for each non-terminal.

**References**

Keijzer, M., O'Neill, M., Ryan, C. and Cattolico, M. (2002) Grammatical Evolution Rules: The Mod and the Bucket Rule, pp. 123-130. In: Foster, J. A., Lutton, E., Miller, J., Ryan, C. and Tettamanzi, A. (Eds.): Genetic Programming. Lecture Notes in Computer Science, Vol.2278, Springer, Heidelberg. <doi:10.1007/3-540-45984-7\_12>

**See Also**

Other Utility: [ChoiceVector\(\)](#)

**Examples**

```
library(xegaBNF)
g<-compileBNF(booleanGrammar())
mLCMG(g$PT$LHS)
```

---

mLCMGCodonPrecision    *mLCMG precision of codon.*

---

**Description**

mLCMG precision of codon.

**Usage**

```
mLCMGCodonPrecision(LHS, ...)
```

**Arguments**

LHS                    Vector of Integers. The left-hand side of a grammar object G.  
 ...                    Unused. Needed for common abstract interface of precision functions.



**Value**

Integer. The precision of a codon whose upper bound is larger than least common multiple of the prime factors of the vector of the available rules for each non-terminal of a grammar.

**See Also**

Other Precision: `CodonPrecisionWithThreshold()`, `MinCodonPrecision()`

**Examples**

```
NT<-sample(5, 50, replace=TRUE)
mLCMGCodonPrecision(NT)
```

---

tLCM

*Computes the largest least common multiple of all prime factors of the integers in the interval 1:m for k-bit integers.*

---

**Description**

For 64 bit numbers, numerically stable up to  $m=42$ . The modulo rule in grammatical evolution assigns to the choices of substitutions for a non-terminal slightly (biased) probabilities. For an integer coding, the least common multiple of all rule choices from no choice (1) to the maximal number of substitutions of a non-terminal removes this bias completely. However, whenever the prime factors of the least common multiple contain a prime different from 2, the bias cannot be removed completely for a binary gene coding. However, each additional bit used for coding approximately halves the bias.

**Usage**

```
tLCM(k)
```

**Arguments**

k                      Number of bits.

**Details**

This could be done with the help of the function `mLCM` of the R-package `numbers`. We implement this by enumerating the vector of prime factors in 1:42.

**Value**

A list of three elements:

- \$k: The number of bits.
- \$m: Maximal number of substitutions for a non-terminal symbol in a grammar.
- \$mLCM: Least common multiple of the prime factors of all rule choices from 1 to \$m.

**See Also**

Other Diagnostics: [CodonChoiceBiasesDeprecated\(\)](#), [CodonChoiceBiases\(\)](#), [CodonPrecision\(\)](#)

**Examples**

```
tLCM(8)
tLCM(16)
tLCM(32)
```

---

xegaGeDecodeGene	<i>Decode a gene for a context free grammar.</i>
------------------	--

---

**Description**

xegaGeDecodeGene() decodes a binary gene with a context-free grammar.

**Usage**

```
xegaGeDecodeGene(gene, lF)
```

**Arguments**

gene	Binary gene.
lF	Local configuration of the genetic algorithm.

**Details**

The codons (k-bit sequences) of the binary gene are determining the choices of non-terminal symbols of a depth-first left-to-right tree traversal. Decoding works in 2 steps:

1. From the binary gene and a grammar a potentially incomplete derivation tree is built.
2. The leaves of the derivation tree are extracted.

It is not guaranteed that a complete derivation trees is returned.

**Value**

Decoded gene.

**See Also**

Other Decoder: [xegaGeGeneMapMod\(\)](#), [xegaGeGeneMapMLCM\(\)](#)

**Examples**

```
lFxegaGeGene$GeneMap<-xegaGeGeneMapFactory("Mod")
gene<-xegaGeInitGene(lFxegaGeGene)
xegaGeDecodeGene(gene, lFxegaGeGene)
```

---

xegaGeGene

*Package xegaGeGene.*


---

## Description

The xegaGeGene package provides functions implementing grammatical evolution with binary coded genes:

## Details

- Gene initialization.
- Gene maps for the mod and (approximately) for the bucket rule.
- Grammar-based decoders for binary coded genes.
- Analysis of the interaction of codon precision with the rule choice bias for a given grammar.
- Automatic determination of codon precision with a limited rule choice bias.

## Gene Initialization

The number of bits of a gene are specified by `lF$BitsOnGene()`.

The number of bits of a codon are specified by `lF$CodonPrecision()`.

## Binary Gene Representation

A binary gene is a named list:

- `$gene1` the gene must be a binary vector.
- `$fit` the fitness value of the gene (for `EvalGeneDet` and `EvalGeneU`) or the mean fitness (for stochastic functions evaluated with `EvalGeneStoch`).
- `$evaluated` has the gene been evaluated?
- `$evalFail` has the evaluation of the gene failed?
- `$var` the cumulative variance of the fitness of all evaluations of a gene. (For stochastic functions)
- `$sigma` the standard deviation of the fitness of all evaluations of a gene. (For stochastic functions)
- `$obs` the number evaluations of a gene. (For stochastic functions)

## Abstract Interface of Problem Environment

A problem environment `penv` must provide:

- `$f(parameters, gene, lF)`: Function with a real parameter vector as first argument which returns a gene with evaluated fitness.
- `$genelength()`: The number of bits of the binary coded real parameter vector. Used in `InitGene`.
- `$bitlength()`: A vector specifying the number of bits used for coding each real parameter. If `penv$bitlength()[1]` is 20, then `parameters[1]` is coded by 20 bits. Used in `GeneMap`.
- `$lb()`: The lower bound vector of each parameter. Used in `GeneMap`.
- `$ub()`: The upper bound vector of each parameter. Used in `GeneMap`.

## The Architecture of the xegaX-Packages

The xegaX-packages are a family of R-packages which implement eXtended Evolutionary and Genetic Algorithms (xega). The architecture has 3 layers, namely the user interface layer, the population layer, and the gene layer:

- The user interface layer (package `xega`) provides a function call interface and configuration support for several algorithms: genetic algorithms (`sga`), permutation-based genetic algorithms (`sgPerm`), derivation free algorithms as e.g. differential evolution (`sgde`), grammar-based genetic programming (`sgp`) and grammatical evolution (`sgge`).
- The population layer (package `xegaPopulation`) contains population related functionality as well as support for population statistics dependent adaptive mechanisms and parallelization.
- The gene layer is split in a representation independent and a representation dependent part:
  1. The representation independent part (package `xegaSelectGene`) is responsible for variants of selection operators, evaluation strategies for genes, as well as profiling and timing capabilities.
  2. The representation dependent part consists of the following packages:
    - `xegaGaGene` for binary coded genetic algorithms.
    - `xegaPermGene` for permutation-based genetic algorithms.
    - `xegaDfGene` for derivation free algorithms as e.g. differential evolution.
    - `xegaGpGene` for grammar-based genetic algorithms.
    - `xegaGeGene` for grammatical evolution algorithms.

The packages `xegaDerivationTrees` and `xegaBNF` support the last two packages: `xegaBNF` essentially provides a grammar compiler and `xegaDerivationTrees` an abstract data type for derivation trees.

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## URL

<https://github.com/ageyerschulz/xegaGeGene>

## Installation

From CRAN by `install.packages('xegaGeGene')`

## Author(s)

Andreas Geyer-Schulz

## References

- Ryan, Conor and Collins, J. J. AND Neill, Michael O. (1998) Grammatical evolution: Evolving programs for an arbitrary language. In: Banzhaf, Wolfgang and Poli, Riccardo, Schoenauer, Marc and Fogarty, Terence C. (1998): Genetic Programming. First European Workshop, EuroGP' 98 Paris, France, April 14-15, 1998 Proceedings, Lecture Notes in Computer Science, 1391, Springer, Heidelberg. <doi:10.1007/BFb0055930>
- O'Neil, Michael AND Ryan, Conor (2003) Grammatical Evolution: Evolutionary Automatic Programming in an Arbitrary Language. Kluwer, Dordrecht. <ISBN:1-4020-7444-1>
- Ryan, Conor and O'Neill, Michael and Collins, J. J. (2018) Handbook of Grammatical Evolution. Springer International Publishing, Cham. <doi:10.1007/978-3-319-78717-6>

---

xegaGeGeneMapFactory    *Configure the gene map function of a genetic algorithm for grammar evolution.*

---

## Description

xegaGeGeneMapFactory() implements the selection of one of the GeneMap functions in this package by specifying a text string. The selection fails ungracefully (produces a runtime error), if the label does not match. The functions are specified locally.

Current support:

1. "Mod" returns GeneMapMod(). (Default).
2. "Bucket" returns GeneMapmLCM().

## Usage

```
xegaGeGeneMapFactory(method = "Mod")
```

## Arguments

method                      String specifying the GeneMap function.

## Value

Gene map function for genes.

## See Also

Other Configuration: [xegaGePrecisionFactory\(\)](#)

## Examples

```
XGene<-xegaGeGeneMapFactory("Mod")
gene<-xegaGeInitGene(1FxegaGeGene)
XGene(gene$gene1, 1FxegaGeGene)
```

---

xegaGeGeneMapmLCM      *Map the bit strings of a binary gene to integer parameters in the interval 1 to numbers::mLCM(x) < 2^k.*

---

### Description

xegaGeGeneMapmLCM() maps the bit strings of a binary string to integers in the interval 1 to 1F\$CodonPrecision(). Bit vectors are mapped into equispaced numbers in the interval.

### Usage

```
xegaGeGeneMapmLCM(gene, 1F)
```

### Arguments

gene	Binary gene (the genotype).
1F	Local configuration.

### Details

Using the interval of 1 to numbers::mLCM(1:m) provides a the least common multiple of all prime factors of the numbers in the interval 1:m. This corresponds to the bucket rule of Keijzer et al. (2002). For 16-bit precision, the highest number of rules for the same non-terminal symbols is 12. For 8-bit precision, this reduces to 6. With 64-bit integer arithmetic, the bucket rule works up to 42 rules starting with the same non-terminal.

### Value

Integer vector.

### References

Keijzer, M., O'Neill, M., Ryan, C. and Cattolico, M. (2002) Grammatical Evolution Rules: The Mod and the Bucket Rule, pp. 123-130. In: Foster, J. A., Lutton, E., Miller, J., Ryan, C. and Tettamanzi, A. (Eds.): Genetic Programming, Lecture Notes in Computer Science, Vol.2278, Springer, Heidelberg. <doi:10.1007/3-540-45984-7\_12>

### See Also

Other Decoder: [xegaGeDecodeGene\(\)](#), [xegaGeGeneMapMod\(\)](#)

### Examples

```
gene<-xegaGeInitGene(1FxegaGeGene)
xegaGeGeneMapmLCM(gene$gene1, 1FxegaGeGene)
```

---

xegaGeGeneMapMod	<i>Map the bit strings of a binary gene to parameters in the interval 1:2<sup>k</sup>.</i>
------------------	--

---

### Description

xegaGeGeneMapMod() maps the bit strings of a binary string to integers in the interval 1 to 1F\$CodonPrecision(). Bit vectors are mapped into equispaced numbers in the interval.

### Usage

```
xegaGeGeneMapMod(gene, 1F)
```

### Arguments

gene	Binary gene (the genotype).
1F	Local configuration.

### Details

The modulo rule of grammatical evolution produces (slightly) biased choices of rules with this mapping. The bias goes to zero as 1F\$CodonPrecision() >> number of rules to choose from.

### Value

Integer vector.

### References

Keijzer, M., O'Neill, M., Ryan, C. and Cattolico, M. (2002) Grammatical Evolution Rules: The Mod and the Bucket Rule, pp. 123-130. In: Foster, J. A., Lutton, E., Miller, J., Ryan, C. and Tettamanzi, A. (Eds.): Genetic Programming. Lecture Notes in Computer Science, Vol.2278, Springer, Heidelberg. <doi:10.1007/3-540-45984-7\_12>

### See Also

Other Decoder: [xegaGeDecodeGene\(\)](#), [xegaGeGeneMapmLCM\(\)](#)

### Examples

```
gene<-xegaGeInitGene(1FxegaGeGene)
xegaGeGeneMapMod(gene$gene1, 1FxegaGeGene)
```

---

xegaGeInitGene      *Initialize a binary gene*

---

### Description

xegaGeInitGene() generates a random binary gene with a given length.

### Usage

```
xegaGeInitGene(lF)
```

### Arguments

lF                    the local configuration of the genetic algorithm

### Details

In the binary representation of package xega, *gene* is a list with

1. *\$evaluated* Boolean: TRUE if the fitness is known.
2. *\$fit* The fitness of the genotype of *\$gene1*
3. *\$gene1* a bit string (the genetopye).

This representation makes several code optimizations and generalizations easier.

### Value

a binary gene (a named list):

- *\$evaluated*: FALSE. See package xegaEvalGene
- *\$evalFail*: FALSE. Set by the error handler(s) in package xegaEvalGene in the case of failure.
- *\$fit*: Fitness vector.
- *\$gene1*: Binary gene.

### Examples

```
xegaGeInitGene(lFxegaGeGene)
```



---

`xegaGePrecisionFactory`*Configure the function for computing the codon precision for grammar evolution.*

---

**Description**

`xegaGePrecisionFactory()` implements the selection of one of the functions for computing the codon precision in this package by specifying a text string. The selection fails ungracefully (produces a runtime error), if the label does not match. The functions are specified locally.

Current support:

1. "Min" returns `MinCodonPrecision`. Shortest coding, but some choice bias.
2. "LCM" returns `mLCMGCodonPrecision`. (Default)
3. "MaxPBias" returns `CodonPrecisionWithThreshold`.

**Usage**

```
xegaGePrecisionFactory(method = "LCM")
```

**Arguments**

`method`               String specifying the GeneMap function.

**Value**

Precision of codon function.

**See Also**

Other Configuration: [xegaGeGeneMapFactory\(\)](#)

**Examples**

```
CodonPrecision<-xegaGePrecisionFactory("Min")
NT<-sample(5, 50, replace=TRUE)
CodonPrecision(NT)
CodonPrecision<-xegaGePrecisionFactory("MaxPBias")
CodonPrecision(NT, 0.1)
```

# Index

## \* Configuration

xegaGeGeneMapFactory, [13](#)  
xegaGePrecisionFactory, [17](#)

## \* Decoder

xegaGeDecodeGene, [10](#)  
xegaGeGeneMapmLCM, [14](#)  
xegaGeGeneMapMod, [15](#)

## \* Diagnostics

CodonChoiceBiases, [3](#)  
CodonChoiceBiasesDeprecated, [4](#)  
CodonPrecision, [5](#)  
tLCM, [9](#)

## \* Gene Generation

xegaGeInitGene, [16](#)

## \* Package Description

xegaGeGene, [11](#)

## \* Precision

CodonPrecisionWithThreshold, [5](#)  
MinCodonPrecision, [7](#)  
mLCMGCodonPrecision, [8](#)

## \* Utility

ChoiceVector, [2](#)  
mLCMG, [7](#)

## \* datasets

lFxegaGeGene, [6](#)

ChoiceVector, [2](#), [8](#)

CodonChoiceBiases, [3](#), [4](#), [5](#), [10](#)

CodonChoiceBiasesDeprecated, [3](#), [4](#), [5](#), [10](#)

CodonPrecision, [3](#), [4](#), [5](#), [10](#)

CodonPrecisionWithThreshold, [5](#), [7](#), [9](#)

lFxegaGeGene, [6](#)

MinCodonPrecision, [6](#), [7](#), [9](#)

mLCMG, [2](#), [7](#)

mLCMGCodonPrecision, [6](#), [7](#), [8](#)

tLCM, [3–5](#), [9](#)

xegaGeDecodeGene, [10](#), [14](#), [15](#)

xegaGeGene, [11](#)

xegaGeGeneMapFactory, [13](#), [17](#)

xegaGeGeneMapmLCM, [10](#), [14](#), [15](#)

xegaGeGeneMapMod, [10](#), [14](#), [15](#)

xegaGeInitGene, [16](#)

xegaGePrecisionFactory, [13](#), [17](#)