

# Package ‘copre’

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**Type** Package

**Title** Tools for Nonparametric Martingale Posterior Sampling

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**Description** Performs Bayesian nonparametric density estimation using Martingale posterior distributions including the Copula Resampling (CopRe) algorithm. Also included are a Gibbs sampler for the marginal Gibbs-type mixture model and an extension to include full uncertainty quantification via a predictive sequence resampling (SeqRe) algorithm. The CopRe and SeqRe samplers generate random nonparametric distributions as output, leading to complete nonparametric inference on posterior summaries. Routines for calculating arbitrary functionals from the sampled distributions are included as well as an important algorithm for finding the number and location of modes, which can then be used to estimate the clusters in the data using, for example, k-means. Implements work developed in Moya B., Walker S. G. (2022). [doi:10.48550/arxiv.2206.08418](https://doi.org/10.48550/arxiv.2206.08418), Fong, E., Holmes, C., Walker, S. G. (2021) [doi:10.48550/arxiv.2103.15671](https://doi.org/10.48550/arxiv.2103.15671), and Escobar M. D., West, M. (1995) [doi:10.1080/01621459.1995.10476550](https://doi.org/10.1080/01621459.1995.10476550).

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copre-package

*CopRe Tools for Nonparametric Martingale Posterior Sampling*

---

### Description

Performs Bayesian nonparametric density estimation using Martingale posterior distributions including the Copula Resampling (CopRe) algorithm. Also included are a Gibbs sampler for the marginal Gibbs-type mixture model and an extension to include full uncertainty quantification via a predictive sequence resampling (SeqRe) algorithm. The CopRe and SeqRe samplers generate random nonparametric distributions as output, leading to complete nonparametric inference on posterior summaries. Routines for calculating arbitrary functionals from the sampled distributions are included as well as an important algorithm for finding the number and location of modes, which can then be used to estimate the clusters in the data using, for example, k-means. Implements work developed in Moya B., Walker S. G. (2022).

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## References

- Fong, E., Holmes, C., Walker, S. G. (2021). Martingale Posterior Distributions. arXiv. DOI: [doi:10.48550/arxiv.2103.15671](https://doi.org/10.48550/arxiv.2103.15671)
- Moya B., Walker S. G. (2022). Uncertainty Quantification and the Marginal MDP Model. arXiv. DOI: [doi:10.48550/arxiv.2206.08418](https://doi.org/10.48550/arxiv.2206.08418)
- Escobar M. D., West, M. (1995) Bayesian Density Estimation and Inference Using Mixtures. Journal of the American Statistical Association. DOI: [doi:10.1080/01621459.1995.10476550](https://doi.org/10.1080/01621459.1995.10476550)

---

antimodes

*Antiode Extractor*

---

## Description

Extracts the antimodes from a `copre_result` or `secre_result` object.

## Usage

```
antimodes(obj, mean = FALSE, grd = NULL, idx = FALSE)
```

## Arguments

<code>obj</code>	A <code>copre_result</code> or <code>mdp_result</code> object.
<code>mean</code>	A logical value indicating whether to extract the modes of the mean density of each of the individual sampled density.
<code>grd</code>	For <code>mdpolya_result</code> , a grid on which to evaluate the object.
<code>idx</code>	A logical value indicating whether to also return the index within <code>grd</code> of the discovered modes.

## Value

A matrix of antimodes values in the support of the `copre_result` density

---

`autoplot.copre_result` *Create a CopRe Result ggplot*

---

## Description

Create a CopRe Result ggplot

## Usage

```
autoplot.copre_result(x, ..., func = "density", confint = NULL)
```

**Arguments**

x	A copre_result object.
...	Additional arguments discarded from plot.
func	Either 'distribution', 'density', or 'gradient'.
confint	A decimal value indicating the confidence interval width (e.g. 0.95 for a 95% confidence interval). Defaults to NULL, in which case no confidence intervals will be drawn.

**Value**

A ggplot object.

---

autoplot.grideval\_result

*Create a ggplot of a grideval\_result Object*

---

**Description**

Create a ggplot of a grideval\_result Object

**Usage**

```
autoplot.grideval_result(x, ..., confint = NULL)
```

**Arguments**

x	A grideval_result object.
...	Additional arguments discarded from plot.
confint	A decimal value indicating the confidence interval width (e.g. 0.95 for a 95 percent confidence interval). Defaults to NULL, in which case no confidence intervals will be drawn.

**Value**

A ggplot object.

---

autoplot.seqre\_result *Create a SeqRe Result ggplot*

---

### Description

Create a SeqRe Result ggplot

### Usage

```
autoplot.seqre_result(x, ..., func = "density", confint = NULL)
```

### Arguments

x	A seqre_result object.
...	Additional arguments discarded from plot.
func	Either 'distribution', 'density', or 'gradient'.
confint	A decimal value indicating the confidence interval width (e.g. 0.95 for a 95% confidence interval). Defaults to NULL, in which case no confidence intervals will be drawn.

### Value

A ggplot object.

---

base_measure	<i>Base Measure for Mixture Models</i>
--------------	--

---

### Description

A structure for wrapping base measures as in Escobar and West (1995).

### Usage

```
base_measure(idx, dim, pars, hpars, eval)
```

### Arguments

idx	A unique index for the base measure.
dim	A dimension for the support of the base measure.
pars	A list of parameters used to generate mixture components.
hpars	A list of hyperparameters used to generate pars.
eval	An evaluation function taking phi, a list of mixture parameter matrices, grd, a grid vector, f, a character string indicating whether to calculate the gradient, density, or distribution function, and nthreads, a number of threads to utilize for parallel execution.

**Value**

A base\_measure object for use in the sequence resampling scheme for mixtures.

**References**

- Escobar M. D., West, M. (1995) Bayesian Density Estimation and Inference Using Mixtures. Journal of the American Statistical Association. DOI: [doi:10.1080/01621459.1995.10476550](https://doi.org/10.1080/01621459.1995.10476550)

**See Also**

[seqre\(\)](#)

---

copre

*Copula Resampling*

---

**Description**

A function that samples predictive distributions for univariate continuous data using the bivariate Gaussian copula.

**Usage**

```
copre(  
  data,  
  N,  
  k,  
  rho = 0.91,  
  grd_res = 1000,  
  nthreads = parallel::detectCores(),  
  gpu = FALSE,  
  gpu_path = NULL,  
  gpu_ouir = NULL,  
  gpu_seed = 1234  
)
```

**Arguments**

data	The data from which to sample predictive distributions.
N	The number of unobserved data points to resample for each chain.
k	The number of predictive distributions to sample.
rho	A scalar concentration parameter.
grd_res	The number of points on which to evaluate the predictive distribution.
nthreads	The number of threads to call for parallel execution.
gpu	A logical value indicating whether or not to use the CUDA implementation of the algorithm.

gpu_path	The path to the CUDA implementation source code.
gpu_ouir	A directory to output the compiled CUDA code.
gpu_seed	A seed for the CUDA random variates.

**Value**

A `copre_result` object, whose underlying structure is a list which contains the following components:

**References**

Fong, E., Holmes, C., Walker, S. G. (2021). Martingale Posterior Distributions. arXiv. DOI: [doi:10.48550/arxiv.2103.15671](https://doi.org/10.48550/arxiv.2103.15671)

**Examples**

```
res_cop <- copre(rnorm(50), 10, 10, nthreads = 1)
```

---

functional

*Obtain Functionals from a CopRe Result*


---

**Description**

Obtain Functionals from a CopRe Result

**Usage**

```
functional(obj, f, ..., mean = FALSE)
```

**Arguments**

obj	A <code>copre_result</code> object.
f	A list of functions.
...	Additional arguments passed to f.
mean	A logical value indicating whether or not to obtain the functional from the point-wise mean of the sampled distributions or from each individually.

**Value**

The integral over the `copre_result` grid of the functions in the list multiplied by the density of each sample distribution in `obj`.

---

 gibbsmix

*Marginal Gibbs-type Mixture Model Sampler*


---

**Description**

A function that samples marginal mixture densities via a marginal Gibbs sampler.

**Usage**

```
gibbsmix(data, k, b_msr, s_msr, burn = 1000, thin = 150)
```

**Arguments**

data	The data from which to sample predictive distributions.
k	The number of predictive samples to draw.
b_msr	A base_measure object.
s_msr	A seq_measure object.
burn	The number of initial sampling iterations to discard, will be truncated if a non-integer.
thin	The number of sampling iterations to discard between records, will be truncated if a non-integer.

**Value**

A seqre\_result object.

**See Also**

[seqre\(\)](#), [seq\\_measure\(\)](#), [base\\_measure\(\)](#)

---

 G\_normls

*Normal-Inverse-Gamma Base Measure for Location-Scale Normal Mixture Models.*


---

**Description**

Normal-Inverse-Gamma Base Measure for Location-Scale Normal Mixture Models.

**Usage**

```
G_normls(mu = 0, tau = 1, s = 1, S = 1, a = NULL, A = NULL, w = NULL, W = NULL)
```



**Arguments**

mu	The mean parameter.
tau	The variance scaling parameter.
s	The primary shape parameter for the Inverse-Gamma component.
S	The secondary shape parameter for the Inverse-Gamma component.
a	The prior mean parameter for mu.
A	The prior variance for mu.
w	The prior primary shape parameter for tau.
W	The prior secondary shape parameter for tau.

**Value**

A base\_measure object for use in the sequence resampling scheme for mixtures.

**See Also**

[base\\_measure\(\)](#), [seqre\(\)](#)

---

length.grideval\_result

*Length*

---

**Description**

Length

**Usage**

```
## S3 method for class 'grideval_result'
length(x)
```

**Arguments**

x                    A grideval\_result object.

**Value**

The number of samples k in obj.

---

 modes

---

*Mode Extractor*


---

### Description

Extracts the modes from a `copre_result` or `secre_result` object.

### Usage

```

modes(obj, mean = FALSE, grd = NULL, idx = FALSE, anti = FALSE)

## S3 method for class 'secre_result'
modes(obj, mean = FALSE, grd = NULL, idx = FALSE, anti = FALSE)

## S3 method for class 'grideval_result'
modes(obj, mean = FALSE, grd = NULL, idx = FALSE, anti = FALSE)

n_modes(obj, mean = FALSE, grd = NULL, anti = FALSE)

```

### Arguments

<code>obj</code>	A <code>copre_result</code> or <code>secre_result</code> object.
<code>mean</code>	A logical value indicating whether to count the modes of the mean density of each of the individual sampled density.
<code>grd</code>	For <code>secre_result</code> , a grid on which to evaluate the object.
<code>idx</code>	A logical value indicating whether to also return the index within <code>grd</code> of the discovered modes.
<code>anti</code>	A logical value indicating whether to extract true modes or anti-modes (i.e. local minima of the density function).

### Value

A matrix of modes values in the support of the `copre_result` density

### Methods (by class)

- `modes(secre_result)`: Mode-counting method for `secre_result` objects.
- `modes(grideval_result)`: Mode-counting method for `grideval_result` objects.

### Functions

- `n_modes()`: Counts the modes from a `copre_result` or `secre_result` object.

---

moment	<i>Obtain Moments from a CopRe or SeqRe Result</i>
--------	--

---

**Description**

Obtain Moments from a CopRe or SeqRe Result

**Usage**

```
moment(obj, mom, cntrl = TRUE, grd = NULL)

## S3 method for class 'secre_result'
moment(obj, mom, cntrl = TRUE, grd = NULL)

## S3 method for class 'grideval_result'
moment(obj, mom, cntrl = TRUE, grd = NULL)
```

**Arguments**

obj	A copre_result or secre_result object.
mom	A numeric scalar indicating the moment to calculate.
cntrl	A logical value indicating whether the moment should be central or not. Defaults to TRUE.
grd	A numeric vector of grid values on which the density function samples in obj should be calculated for trapezoidal integration.

**Value**

A vector of moment values for each sampled distribution in obj.

**Methods (by class)**

- `moment(secre_result)`: Moment calculation method for secre\_result objects.
- `moment(grideval_result)`: Moment calculation method for grideval\_result objects.

---

plot.copre_result	<i>Create a CopRe Result Plot</i>
-------------------	-----------------------------------

---

**Description**

Create a CopRe Result Plot

**Usage**

```
## S3 method for class 'copre_result'
plot(x, ..., func = "density", confint = NULL, use_ggplot = TRUE)
```

**Arguments**

x	A copre_result object.
...	Additional arguments discarded from plot.
func	Either 'distribution', 'density', or 'gradient'.
confint	A decimal value indicating the confidence interval width (e.g. 0.95 for a 95% confidence interval). Defaults to NULL, in which case no confidence intervals will be drawn.
use_ggplot	A logical value indicating whether to use ggplot2 instead of the base plot function.

**Value**

None.

---

plot.grideval\_result *Create a Plot of a grideval\_result Object*

---

**Description**

Create a Plot of a grideval\_result Object

**Usage**

```
## S3 method for class 'grideval_result'
plot(x, ..., confint = NULL, use_ggplot = TRUE)
```

**Arguments**

x	A grideval_result object.
...	Additional arguments discarded from plot.
confint	A decimal value indicating the confidence interval width (e.g. 0.95 for a 95 percent confidence interval). Defaults to NULL, in which case no confidence intervals will be drawn.
use_ggplot	A logical value indicating whether to use ggplot2 instead of the base plot function.

**Value**

A ggplot object if ggplot2 is used, else none.

---

plot.seqre\_result      *Create a SeqRe Result Plot*

---

### Description

Create a SeqRe Result Plot

### Usage

```
## S3 method for class 'seqre_result'  
plot(x, ..., func = "density", confint = NULL, use_ggplot = TRUE)
```

### Arguments

x	A seqre_result object.
...	Additional arguments discarded from plot.
func	Either 'distribution', 'density', or 'gradient'.
confint	A decimal value indicating the confidence interval width (e.g. 0.95 for a 95% confidence interval). Defaults to NULL, in which case no confidence intervals will be drawn.
use_ggplot	A logical value indicating whether to use ggplot2 instead of the base plot function.

### Value

None.

---

registerautoplot\_s3\_methods  
*Register autoplot methods to ggplot2*

---

### Description

Register autoplot methods to ggplot2

### Usage

```
registerautoplot_s3_methods()
```

### Value

None

---

register\_s3\_method      *Register S3 Methods from External Packages*

---

**Description**

<https://github.com/tidyverse/hms/blob/master/R/zzz.R>

**Usage**

```
register_s3_method(pkg, generic, class, fun = NULL)
```

**Arguments**

pkg	Package name.
generic	Generic function name.
class	Class name.
fun	Optional custom function name.

**Value**

None

---

seq\_measure      *Sequence Measure for Species Sampling Models*

---

**Description**

Sequence Measure for Species Sampling Models

**Usage**

```
seq_measure(idx, pars, hpars, Pn, Po)
```

**Arguments**

idx	A unique index for the sequence measure.
pars	A list of parameters used in Pn and Po to generate a sequence.
hpars	A list of hyperparameters used to generate pars.
Pn	A function on a sequence length n and a number of unique values k that returns the probability of the next member in the sequence having a new value.
Po	A function on a sequence length n, a number of unique values k, and the number of values equal to j, kj, that returns the probability of the next member in the sequence having the value j.

**Value**

A seq\_measure object for use in the exchangeable sequence resampling scheme for mixtures.

**See Also**

[seqre\(\)](#)

---

Sq_dirichlet	<i>Dirichlet Sequence Measure.</i>
--------------	------------------------------------

---

**Description**

Dirichlet Sequence Measure.

**Usage**

```
Sq_dirichlet(alpha = 1, c = NULL, C = NULL)
```

**Arguments**

alpha	The concentration parameter for the Dirichlet process. Must be greater than 0.
c	The prior primary shape parameter for alpha.
C	The prior secondary shape parameter for alpha.

**Value**

A seq\_measure object for use in the exchangeable sequence resampling scheme for mixtures.

**See Also**

[seq\\_measure\(\)](#), [seqre\(\)](#)

---

Sq_gnedin0	<i>Collapsed Gnedin Process Sequence Measure.</i>
------------	---

---

**Description**

Collapsed Gnedin Process Sequence Measure.

**Usage**

```
Sq_gnedin0(gamma)
```

**Arguments**

gamma            The gamma parameter for the Gnedin process with xi set to 0. Bounded to  $[0, 1]$ .

**Value**

A seq\_measure object for use in the exchangeable sequence resampling scheme for mixtures.

**See Also**

[seq\\_measure\(\)](#), [seqre\(\)](#)

---

Sq\_pitmanyor

*Pitman-Yor Sequence Measure.*

---

**Description**

Pitman-Yor Sequence Measure.

**Usage**

```
Sq_pitmanyor(d, alpha = 1, m = 1L)
```

**Arguments**

d                The discount parameter for the Pitman-Yor process. Must be less than 1.

alpha            The concentration parameter for the Pitman-Yor process. Must be greater than  $-\sigma$  if  $\sigma$  is in  $[0, 1)$ , else ignored.

m                A positive integer used to set  $\theta = m * \text{abs}(\sigma)$  if  $\sigma$  is negative.

**Value**

A seq\_measure object for use in the exchangeable sequence resampling scheme for mixtures.

**See Also**

[seq\\_measure\(\)](#), [seqre\(\)](#)



---

[[.seqrerresult      *Sequence Resampling*

---

### Description

A function that samples predictive distributions for univariate continuous data using exchangeable predictive extension.

### Usage

```
## S3 method for class 'seqrerresult'
obj[[i]]

secre(obj, inc = 1000, eps = 0.001, max_it = 100)
```

### Arguments

obj	A <code>secre_result</code> object, usually output from <code>gibbsmix()</code> .
i	A numeric vector of sample indices.
inc	A positive integer increment value for the number of predictive samples to take each convergence check.
eps	An error value which determines the convergence approximation.
max_it	A positive integer maximum number of iterations before halting.

### Value

A `secre_result` object, or a list of two `secre_result` objects if `keep_marg` is `TRUE`.

### Functions

- `[[`: Subset method for `secre_result` objects

### See Also

[gibbsmix\(\)](#)

---

\$.grideval\_result      *Grid evaluation of copre\_result and seqre\_result objects*

---

### Description

Grid evaluation of copre\_result and seqre\_result objects

### Usage

```
## S3 method for class 'grideval_result'
obj$name

## S3 method for class 'grideval_result'
obj[[i]]

grideval(obj, grd = NULL, func = "density", nthreads = 1)

## S3 method for class 'copre_result'
grideval(obj, grd = NULL, func = "density", nthreads = 1)

## S3 method for class 'seqre_result'
grideval(obj, grd = NULL, func = "density", nthreads = 1)
```

### Arguments

obj	A copre_result or seqre_result object.
name	The name of the attribute to access (i.e. func, grid, or args).
i	A numeric vector of sample indices.
grd	For seqre_result objects, a numeric vector of m grid points.
func	Either 'distribution', 'density', or 'gradient'.
nthreads	The number of parallel threads to launch with OpenMP.

### Value

A grideval\_result object, which is a matrix with dimension  $[k, m]$  of evaluated sample functions, with the following attributes:

- func: The evaluated function.
- grid: The grid points on which each of the k rows was evaluated.
- args: A copy of the args entry from obj.

### Methods (by class)

- grideval(copre\_result): Grid evaluation method for copre\_result objects.
- grideval(seqre\_result): Grid evaluation method for seqre\_result objects.

**Functions**

- `$`: Attribute access method for `grideval_result` objects
- `[]`: Subset method for `grideval_result` objects

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